Second Edition

Financial Algebra

ADVANCED ALGEBRA WITH FINANCIAL APPLICATIONS



Robert Gerver | Richard Sgroi



Australia • Brazil • Mexico • Singapore • United Kingdom • United States

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Dr. Gerver



Dr. Sgroi

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Financial Algebra, Second Edition, aligns to the Common Core State Standards for Mathematical Content.

The CCSS provides clear and consistent guidelines so students, teachers, administrators, and parents have an awareness of the mathematics proficiencies expected and how to attain them. The standards are designed to be rigorous and relevant to the real world, reflecting the knowledge and skills that students need for future success.

The CCSS Domain and Standard are identified to demonstrate that Financial Algebra, Second Edition, addresses at least one, if not several, core standard in each section.

Conceptual Categories

- Number and Quantity
 Modeling
 Geometry

Algebra

- Functions
 Statistics and Probability

A complete correlation of Financial Algebra, Second Edition, to the CCSS for Mathematical Content is available on the community website.

www.cengage.com/financial_alg2e

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MATH TOPICS

Bimodal data Percent
Bivariate data Percentage
Causal relationship Percentile
Correlation Percentile rank
Correlation coefficient Percentiles
Cumulative frequency Range
Domain Raw scores

Explanatory, response, lurking variables Relative cumulative frequency Frequency distribution Relative frequency

 Independent and dependent variables
 Scatter plot

 Interpolation and extrapolation
 Sigma notation

 Linear regression analysis
 Skewed data

Linear regression equation Spreadshee
Mean absolute deviation Standard de
Mean deviation Trend

Measures of central tendency – mean, median, mode Normal curve

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Spreadsheets and formulas Standard deviation Trend

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Variance
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MATH TOPICS

Antilogarithm Literal equations Arithmetic sequence Logarithm Logarithmic equation Change-of-base formula Common logarithm Logarithmic form Compound interest Natural logarithm Continuous compounding One-to-one property of logarithms Exponential decay Patterns and conjectures **Exponential equations** Power property of logarithms **Exponential form** Recursive and iterative thinking Exponential growth Spreadsheets and formulas Limits

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MATH TOPICS

Average daily balance

Cubic equation

Mean

Cubic regression equation

Exponential base e

Exponential equations

Linear equations

Linear regression equation

Spreadsheets and formulas

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MATH TOPICS

Metric System Chord Circle Middle ordinate Projectile motion Circumference Common ratio **Proportions** Conditional probability formula Quadratic equation Radius Diameter Ratios Domain **English Standard System** Slope

English Standard System

Exponential decay

Slope intercept form of a linear equation

Exponential depreciation

Exponential function

Exponential regression

System of linear equations

System of linear, exponential equations

Geometric sequences Two-way tables
Independent events Venn diagrams
Intersection point x-intercept, y-intercept
Linear equations

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MATH TOPICS

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Cusps Literal expressions
Domain Piecewise functions
Exponential functions Percent

Geometric sequence Spreadsheets and formulas Graphs of functions

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MATH TOPICS

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Compound inequality notation

Domain

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Slope, intercept form of a linear equation

Interval notation

Spreadsheets and formulas

Linear equation

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MATH TOPICS

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MATH TOPICS

Objective function Axis of symmetry Parabola Bias Quadratic equation Completing the square method Complex number Quadratic formula Complex roots Random number tables Experimental design Roots of a quadratic equation Roots, zeros of a quadratic equation Hypothesis testing Imaginary unit Sampling Inequality constraints Surveying Leading coefficient System of linear equations System of linear, quadratic equations Linear equation Linear programming Unbiased estimators Literal quadratic equation Minimum, maximum

> Percent increase **Percents** Pie charts Probability Rational equations Spreadsheets

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MATH TOPICS Addition, subtraction of matrices Matrix Matrix multiplication Array Bar graph Piecewise functions Central angle Ratio Circle graph Scalar Dimensions of a matrix Scalar multiplication Element of a matrix Sector Greatest integer function Spreadsheets and formulas Inequalities Zero matrix Line graph

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New to this Edition

Note: The code "FA1E" refers to the first edition of *Financial Algebra* and the section number from the first edition follows.

Chapter 1 Discretionary Expenses

- **1-3** Categorizing Expenses—Discretionary vs. essential expenses measures of central tendency and frequency distributions
- **1-4** Vacation Travel Expenses—cumulative and relative frequency, percentiles
- 1-3 Entertainment Expenses—plays, movies, concerts, out to eat, video games, music downloads, sports events, amusement parks measures of spread
- **1-4** Vacation Destination Expenses—normal curve and z-scores
- **1-5** Personal Expenses—linear regression and scatterplots

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- 2-2 Reconcile a Bank Statement FA1E 3-2
- **2-3** Savings Accounts—intro arithmetic sequences with constant addition plus FA1E 3-3
- **2-4** Explore Compound Interest FA1E 3-4
- **2-5** Compound Interest Formula FA1E 3-5
- **2-6** Continuous Compounding limits of rational functions, plus FA1E 3-6
- **2-7** Future Value of Investments FA1E 3-7
- 2-8 Present Value of Investments FA1E 3-8
- **2-9** The Term of a Single Deposit Account—new section—logarithms plus
- **2-10** The Terms of a Systematic Savings Account—new section—properties of logs

Chapter 3 Consumer Credit

- 3-1 Introduction to Consumer Credit FA1E 4-1
- **3-2** Loans FA1E 4-2
- 3-3 Student Loans—new section
- 3-4 Loan Calculations and Regression FA1E 4-3

- 3-5 Credit Cards FA1E 4-4
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- 4-4 Probability: The Basis of Insurance—
 conditional probability, independent events,
 Venn diagrams –NEW SECTION
- **4-5** Linear Automobile Depreciation FA1E 5-5
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- **4-7** Driving Data FA1E 5-7
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- **7-2** Reading a Floor Plan FA1E 8-2
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- **7-4** Purchasing a Home FA1E 8-4
- **7-5** Mortgage Points new section
- **7-6** Rentals, Condominiums, and Cooperatives FA1E 8-5
- **7-7** Home Maintenance and Improvement—new section: trig and pythag, similar triangles

Chapter 8 The Stock Market

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- **8-7** Stock Transaction Fees FA1E 1-7
- **8-8** Stock Splits FA1E 1-8
- 8-9 Dividend Income FA1E 1-9

Chapter 9 Modeling a Business

- **9-1** Inventions—surveying, critiquing experimental designs, bias new section
- **9-2** Market Research—unbiased estimators, sampling, types of samples, critiquing experimental design methods new section

- 9-3 Supply and Demand FA1E 2-3
- 9-4 Fixed and Variable Expenses FA1E 2-4
- **9-5** Graphs of Expense and Revenue Functions completing the square plus FA1E 2-5
- 9-6 Breakeven Analysis FA1E 2-6
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Chapter 10 Planning for Retirement

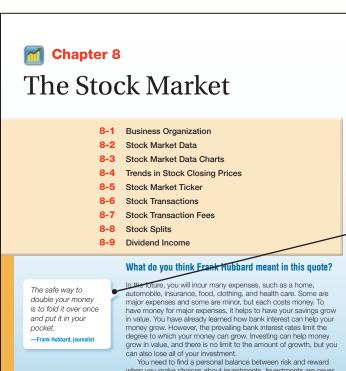
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Inside the Student Edition

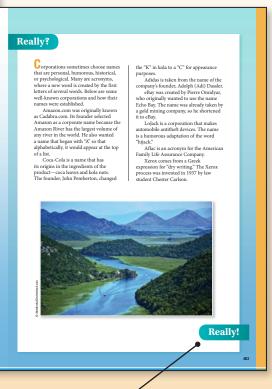


A relevant quote and chapter introduction set the stage for the topics covered in the chapter.

You need to find a personal balance between risk and reward when you make choices about investments. Investments are never without questions. Did you miss the chance to make more money

without questions. Did you miss the chance to make more money because you were being overly cautious? Was the investment too riskly? Did you risk losing principal by investing in something that may not have had a sound foundation? Investors struggle with these questions every day. The stock market is a forum in which the investment risk/reward balance is put to the test. Will the market advance? Will the market decline? No one can be certain. Will the corporations you choose flourish, grow, and succeed, or falter? With a strong knowledge of the stock market, corporations, and investment strategies, you as an investor can make decisions that are based on experience, data, trends, and mathematics.

"This information is interesting and relevant! Showing real-world relevance is always a good lead into the section."



Really? Really! captures students' attention by discussing a fascinating real-life topic that relates to the chapter's content.

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Structure Puts Math into Context

8-1 Business Organization

Genius is 1% inspiration and 99% perspiration. Accordingly, a genius is often merely a talented person who has done all of his or her homework.

- State the basic vocabulary of business organizations.
 Compute financial responsibility of the state of the s
- business ownership based on ratios and percentages.

Key Terms

capital sole proprietorship

personally liable partnership

shareholders private corporation public corporation

Warm-Up

Create and solve an equation models the following relations are some control of the control of t

terms of x.
Find two consecutive integers such that
the sum of three times the first and twice
the second is 27.

A list of **objectives** provides the main learning outcomes for the

basic concepts.

chapter.

Warm-Up provides a refresher for

How Do Businesses Start?

Think of everything you use on a daily basis, from complex electronic devices to simple items like straws, paper clips, and toothbrushes. Have you ever wondered who invented them, or how each has been improved upon? Some inventions provide an opportunity to build a business, but not all. It takes imagination, money, and effort to create a successful business. The money used to start or expand a business is called capital.

expand a business is called capital.

A business owned by one person is a sole proprietorship. The owner, or proprietor, can hire people to help run the business, but these employees are not owners. The owner is responsible for all expenses, including labor and raw materials used in manufacturing a product or providing a service. The money left after all expenses are paid is profit. The owner of a sole proprietorship is entitled to all of the profits. However, the owner is responsible, or personally liable, for any losses. Even if the business does not make a profit, the owner must still pay all of the bills of the business.

A business that is owned by a group of people, called partners, is a partnership. Partners share the profits and the responsibility for any losses. The partners are personally liable for any losses. Personal liability may require risking personal property. Sole proprietors and partners must consider this possibility

personal property. Sole proprietors and partners must consider this possibility when creating a business.

when creating a business.

A corporation is a business organization that can be owned by one person or a group of people. Each owner who invests money in the corporation receives shares of stock in the corporation. The owners are called shareholders. Stock certificates are used as proof of ownership. Unlike sole proprietorships and partnerships, the shareholders in a corporation have limited liability—each

"An intriguing quote at the beginning of each section motivates learning!"

The best way to deal with credit card debt is to educate yourself.

Mark Rosen, Author

"An interesting introduction and a great metaphor for the section!"

Although it's easy to forget sometimes, a share is not a lottery ticket . . . it's part-ownership of a business.

Peter Lynch, American businessman, Investment strategist, and Philanthropist

Nobody ever lost money taking a profit.

Bernard Baruch, Businessman

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The Essential Question helps focus attention on the big idea

What are social security and medicare?

How do people gain access to money they keep in the bank?

What is compound interest?

What information do you need to know before taking out a loan?

What information does a credit card statement give you?

How do revenue and expenses contribute to profit calculation? The **Essential Question helps** focus attention on the big idea of each section. You will be able to answer the question by the end of the section.

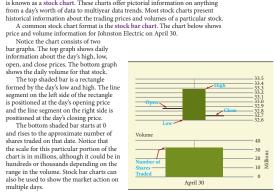
8-3 Stock Market Data Although it's easy to forget sometimes, a share is not a lottery ticket . . . it's part-ownership of a business Key Terms **Objectives** Warm-Up Wathi-OD
An item usually sells for X dollars. It is marked down to Y dollars. Interpret each of the following algebraic expressions in this context.

a. |Y-X|b. |Y-X|/Xc. 100|Y-X|/Xstock chart stock bar chart candlestick chart · Interpret a stock bar chart. · Create a stock bar chart. · Interpret a stock candlestick chart. . Create a stock candlestick chart How Can Stock Data Be Displayed?

Each section begins with a discussion of terms and concepts related to the section topic.

Stock data can be presented in list form or in graphical form. The graphical form is known as a stock chart. These charts offer pictorial information on anything from a day's worth of data to multiyear data trends. Most stock charts present

also be used to show the market action on multiple days.



8-3 Stock Market Data Charts

"This book contains relevant and current information high school students need. The educational focus of today is on standards. This book allows both to be addressed."

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When am I ever going to use this in real life?

owner cannot lose more than the value of his or her share of the business. The number of shareholders in a corporation depends on the structure of the business. When all of the shares are owned solely by a few individuals, and are not available for sale to the public, the corporation is a private corporation, also known as a privately held corporation. The New York Yankees are an example of a private to proporation. So is Lego, Your local car dealership is most likely a private corporation. When anyone can purchase stock in a corporation, the corporation is a public corporation. You might already be familiar with public corporations such as Nike, McDonald's, Xerox, and Apple. These corporations are owned business when the corporation is the public corporations are owned business when the corporation is a public corporation. such as Yinke, MicDianlas, Aerlos, and Applie: Tines coriporations are owned by housewives, doctors, plumbers, teachers, students, senior citizens—anjoine who buys a share in the corporation. If a shareholder owns more than 50% of the shares, that shareholder owns a majority of the shares. The prices of shares of stock in public corporations can be found in newspapers, on television business channels, and on the Internet.

In Skills and Strategies, the heart of the section, math concepts are taught through worked-out examples. Examples present each math concept step-by-step.

Skills and **Strategies**

When a business is owned by more than one person, the owners do not necessarily own equivalent portions of the business. Ratios and percentages can be used to represent the financial responsibility of owners and partners. Recall the relationship between decimals and percentages.

To convert a decimal to a percentage, multiply the decimal by 100 and annex a $\,$ percent sign

To convert a percentage to a decimal, divide the percent by 100 and drop the percent sign.

EXAMPLE 1

Michelle invests \$15,000 in a partnership that has four other partners. The total investment of all partners is \$240,000. What percent of the business does Michelle own?

SOLUTION Represent Michelle's investment as a fraction of the total investment

 $\frac{\text{Michelle's investment}}{\text{Michelle's investment}} = \frac{15,000}{1000}$ Write as a fraction. Total investment 15,000 ÷ 240,000 = 0.0625 Multiply by 100. Write a percent sign. $0.0625 \times 100 = 6.25\%$

Kyle invests \$20,000 in a partnership that has five other partners. The total investment of the partners is \$160,000. What percent of the business is owned by the five other partners?

Michelle owns 6.25% of the partnership.

"I love the emphasis on applications with relevance to the world we live in, not on symbolic manipulation."

The total number of shares of stock in Bulls Corp is 650,000. Mike owns 12% of the shares. How many shares of Bulls Corp stock does he own?

SOLUTION Let x represent the number of shares Mike owns. $12\% = \frac{12}{100}$ Express 12% as a fraction.

 $\frac{12}{100} = \frac{x}{650,000}$ 100x = (12)(650,000)Find the product. 100x = 7,800,000 $\frac{100x}{100} = \frac{7,800,000}{100}$ Divide both sides by 100. Mike owns 78,000 shares of the Bulls Corp.

Check Your Jillian owns 60% of the stock in a private catering corporation. There are 1,200 shares in the entire corporation. How many shares does Jillian own?

Three partners are investing a total of \$900,000 to open a garden and landscaping store. Their investments are in the ratio 2:3:5. How much does the partner that invested the least contribute?

SOLUTION Use the ratio 2:3:5 to write an expression for the amount each partner

Let 2x represent the amount invested by the first partner.

Let 3x represent the amount invested by the second partner. Let 5x represent the amount invested by the third partner. Write an equation showing the three investments total \$900,000.

2x + 3x + 5x = 900,000

The partner that invested the least is represented by the expression 2x. ion. 2(90,000) = 180,000

Check Your Two partners are starting a wedding planning business. The total investment is \$45,000. Their investments are in the ratio 4:5. How much does each investor contribute?

All math concepts are taught within real-life context. When am I ever going to use this in real life? is answered

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Ongoing Assessment and Review

The trading prices for the first three days are A, B, and C. The average of those

 $\frac{A+B+C}{3} = \frac{A}{3} + \frac{B}{3} + \frac{C}{3}$

Using the method in Example 1, find the average of days 2-4 using B, C, and D. This is the same as subtracting price A and adding price D, or

$$\frac{A}{3} + \frac{B}{3} + \frac{C}{3} - \frac{A}{3} + \frac{D}{3}$$

Rearranging the terms and simplifying, this process is the same as finding the

$$\frac{A}{3} - \frac{A}{3} + \frac{B}{3} + \frac{C}{3} + \frac{D}{3} = \frac{B}{3} + \frac{C}{3} + \frac{D}{3} = \frac{B+C+D}{3}$$

EXAMPLE 2

Use the subtraction and addition method to determine the 4-day SMA for the following closing prices.

\$121, \$122, \$120, \$119, \$124, \$128, \$126

SOLUTION Calculate the average closing prices of days 1–4.

Add the first four prices. Divide by 4. $\frac{121 + 122 + 120 + 119}{120 + 120} = 120.50.$

Use subtraction and addition to determine the averages for days 2–5.

Find the averages for days 3-6 and days 4-7.

Use previous average, $\frac{122}{4}$, and $\frac{128}{4}$ $121.25 - \frac{122}{4} + \frac{128}{4} = 122.75$

Use previous average, $\frac{120}{4}$, and $\frac{126}{4}$ $122.75 - \frac{120}{4} + \frac{126}{4} = 124.25$

The simple moving averages are \$120.50, \$121.25, \$122.75, and \$124.25.

Use the subtraction and addition method to determine the 3-day SMA for the closing prices \$28, \$31, \$37, \$38, and \$35,

In Example 2, what would the eighth trading day's closing price have to be so that the next moving average remains the same at \$124.25?

Extend Your Understanding

Check Your

8-4 Trends in Stock Closing Prices

"I like the immediate check of understanding instead of waiting until the end of the chapter."

Check Your Understanding

allows you to immediately practice the concept on your own. The questions are similar to the example and help you gauge your understanding of the skills being taught.

Never try to walk across a river just because it has an average depth of four feet.

Why might the author be warning readers to be cautious of averages? How might these words apply to what you have learned?
 In Exercises 2-5, use the method illustrated in Example 1 to determine the simple moving averages by repeatedly finding sums.

- 2. Determine the 3-day SMA for the 10-conse Angie's List Inc. listed below. \$7.78 \$8.08 \$7.99 \$8.02 \$7.89 \$8.72 \$9.19 \$9.16 \$8.98 \$9.38
- 3. Determine the 5-day SMA for the 10-consecutive-day closing prices for Sherwin-Williams Co listed below.

 \$242.50 \$273.98 \$278.16 \$293.94 \$285.04

\$290.80 \$296.02 \$291.01 \$293.41 \$286.85

\$57.35 \$58.61 \$57.98 \$58.07 \$57.50 \$56.97 \$56.35 \$56.83 \$57.16 \$57.18

Determine the 6-day SMA for the 12-cons Exxon Mobil Corp listed below.

\$92.60 \$92.46 \$92.45 \$91.79 \$93.07 \$89.70 \$89.61 \$89.51 \$90.07 \$88.82 \$89.93 \$88.82

In Exercises 6–9, use the method illustrated in Example 2 to determine moving averages by subtraction and addition.

Determine the 2-day SMA for the 10-consecutive-day closing prices for Western Digital Corp listed below.

\$101.96 \$101.80 \$101.50 \$103.07 \$104.94 \$105.12 \$105.66 \$104.76 \$100.56 \$101.31

7. Determine the 3-day SMA for the 10-consecutive-day closing prices for Procter & Gamble Co listed below.

\$66.21 \$65.90 \$67.05 \$67.03 \$66.80 \$66.65 \$66.65 \$65.80 \$65.92 \$65.21

\$121.69 \$122.85 \$120.70 \$123.61 \$123.18 \$122.03 \$122.82 \$124.14 \$124.92 \$124.06

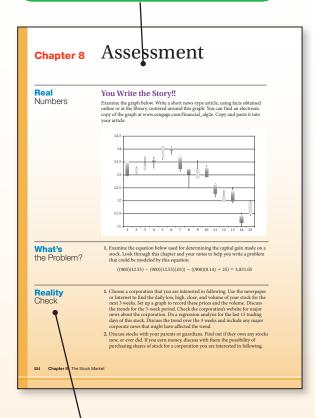
\$2.65 \$2.63 \$2.70 \$2.63 \$2.50 \$2.65 \$2.66 \$2.56 \$2.52 \$2.37

Carefully developed. applications at the end of each section require you to apply the concepts to a specific question or scenario.

Extend Your Understanding provides an opportunity to solve a more challenging problem.

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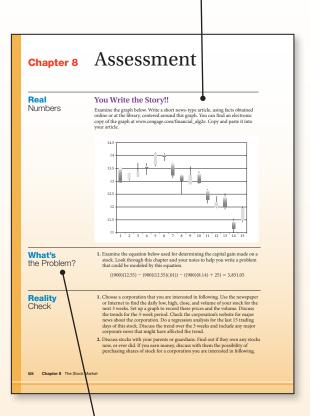
71790_fm_hr_i-xvii.indd 14 12/30/16 2:00 PM **Chapter Assessment** provides an opportunity to check your knowledge of the chapter content.



Reality Check provides specific suggestions for research opportunities, projects, and guest speakers to extend your learning experience.

Real Numbers: You Write the Story!

asks you to examine a graph and write a story focused around the graph's information, giving you an opportunity to be creative while at the same time sharpening your graph interpretation skills.

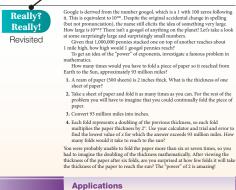


What's The Problem? provides you with a problem posing activity related to a chapter problem. You are given an equation or formula featured in the chapter, with numerical substitutions for each variable. You then have to think backwards and create the problem, using the numbers, that have a solution modeled by the given equation.

"Excellent activities that help connect math to the real world."

XV

Really? Revisited continues the theme of the Really? Really! feature at the beginning of each chapter. In Really? Really! Revisited, you use mathematics to solve a problem or extension related to the Really? Really! theme.



- A ream of paper (500 sheets) is 2 inches thick. What is the thickness of one sheet of paper?
- sneet of paper:

 2. Take a sheet of paper and fold it as many times as you can. For the rest of the problem you will have to imagine that you could continually fold the piece of

many todds would it take to reach to the sun?

You were probably unable to fold the paper more than six or seven times, so you had to imagine the doubling of the thickness mathematically. After viewing the thickness of the paper are is kinds, are you surprised at how few folds it will take the thickness of the paper to reach the sun? The 'power' of 2 is amazing!

- Nick and Matt are partners in a local health food store. They needed \$73,000 to start the business. They invested in the ratio 3?, Nick to Matt.
 How much money did each invest?
 What percent of the business was owned by Matt? Round to the nearest tenth of a percent.

- Tom purchased shares of DuPont for \$47.65 per share. He plans to sell the shares when the stock price rises 20%. At what price will he sell his shares?
- 3. The top three shareholders in a certain corporation each own s shares of stock. The corporation's ownership is represented by a total of x shares of stock. Express the percent of the corporation owned by the top three shareholders algebraically.
- shareholders algebraically.

 4. Marrbed purchased 2,000 shares of stock for \$25.43 per share. She sold them for \$44.10 per share. Express her capital gain to the nearest tenth of a percent.

 5. A local hairstylist bought 450 shares of a cosmetics corporation for \$33.50 per share. He sold the shares for \$30.90 per share.

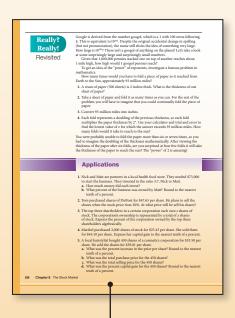
 a. What was the percent increase in the price per sharef Round to the nearest between the process of the price of the 450 shares?

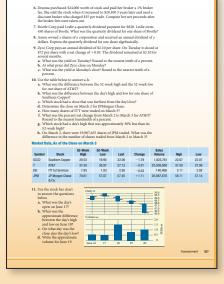
 c. What was the total selling price for the 450 shares?

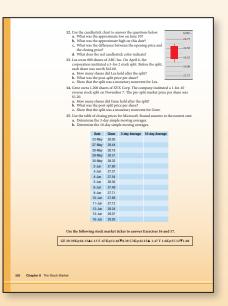
 d. What was the percent capital gain for the 450 shares? Round to the nearest tenth of a percent.

"I love how it is tied to what started the chapter!"

"Great variety of problems that will prepare students for life outside of school!"







Meaningful applications at the end of each chapter require you to apply concepts that were taught throughout the chapter.

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